## - Problem 10.3-05

Let $A$ be the adjacency matrix of a graph $G$ whose vertex set is $\left\{v_{1}, \ldots, v_{n}\right\}$. Prove that the $i$ th entry on the diagonal of $A^{3}$ equals twice the number of different triangles that contain vertex $v_{i}$.

Proof. The $i$ th entry on the diagonal of $A^{3}$ is the number of walks of length 3 from $v_{i}$ to itself. However, a closed walk of length 3 in a graph must give a triangle. Every triangle can be walked in exactly two different directions. Hence, the number of walks of length 3 is twice the number of triangles.

