## - Problem 11.1-07

Solve the Chinese Postman Problem for the unweighted graph shown.


Solution. The six vertices of odd degree are $A, B, C, D, E$ and $F$ in the following figure.
Now, the sum of lengths of shortest paths for all partitions of pairs are given as follows.

| Partition into pairs |  | Sum of lengths of shortest paths |  |
| :---: | :---: | :---: | :---: |
| $\{A, B\},\{C, D\},\{E, F\}$ | $2+3+1=6$ | $\{A, B\},\{C, E\},\{D, F\}$ | $2+3+2=7$ |
| $\{A, B\},\{C, F\},\{D, E\}$ | $2+3+1=6$ | $\{A, C\},\{B, D\},\{E, F\}$ | $3+2+1=6$ |
| $\{A, C\},\{B, E\},\{D, F\}$ | $3+3+2=8$ | $\{A, C\},\{B, F\},\{D, E\}$ | $3+4+1=8$ |
| $\{A, D\},\{B, C\},\{E, F\}$ | $4+3+1=8$ | $\{A, D\},\{B, E\},\{C, F\}$ | $4+3+3=10$ |
| $\{A, D\},\{B, F\},\{C, E\}$ | $4+4+3=11$ | $\{A, E\},\{B, C\},\{D, F\}$ | $5+3+2=10$ |
| $\{A, E\},\{B, D\},\{C, F\}$ | $5+2+3=10$ | $\{A, E\},\{B, F\},\{C, D\}$ | $5+4+3=12$ |
| $\{A, F\},\{B, C\},\{D, E\}$ | $6+3+1=10$ | $\{A, F\},\{B, D\},\{C, E\}$ | $6+2+3=11$ |
| $\{A, F\},\{B, E\},\{C, D\}$ | $6+3+3=12$ |  |  |

So we see that one solution is to add copies of edges $A X, X B, C Y, Y Z, Z D$, and $E F$, as shown.


